

```
In [7]: def queen_safe(row, qsofar):
        """ returns True if it is safe to place another
        queen in `row` in column `len(qsofar)`, given
        existing placement of queens in `qsofar` in the first
        `len(qsofar)` columns """
        col = len(qsofar)
        for (pcol,prow) in enumerate(qsofar):
            # can't place queen in same row
            if prow == row:
                return False
            # diagonal attack
            if abs(prow-row) == col-pcol:
                return False
        # no problems with any existing queens
        return True
```

```
In [11]: def nqueens(n, qsofar=[]):
         col = len(qsofar)
         if col == n:
             return (True,0)
         safe_calls = 0
         for row in range(n):
             safe_calls += 1
             if queen_safe(row, qsofar):
                 result, ncalls = nqueens(n, qsofar + [row])
                 safe_calls += ncalls
                 if result:
                     return (True, safe_calls)
         return (False, safe_calls)
```

```
In [23]: nq_complexity = []
         for n in range(1,30):
             result = nqueens(n)
             print(n, result)
             nq_complexity.append(result[1])
```

```

1 (True, 1)
2 (False, 6)
3 (False, 18)
4 (True, 26)
5 (True, 15)
6 (True, 171)
7 (True, 42)
8 (True, 876)
9 (True, 333)
10 (True, 975)
11 (True, 517)
12 (True, 3066)
13 (True, 1365)
14 (True, 26495)
15 (True, 20280)
16 (True, 160712)
17 (True, 91222)
18 (True, 743229)
19 (True, 48184)
20 (True, 3992510)
21 (True, 179592)
22 (True, 38217905)
23 (True, 584591)
24 (True, 9878316)
25 (True, 1216775)
26 (True, 10339849)
27 (True, 12263400)

```

```

-----
-----
KeyboardInterrupt                                Traceback (most recent call
last)
<ipython-input-23-899f48fb0902> in <module>
      1 nq_complexity = []
      2 for n in range(1,30):
----> 3     result = nqueens(n)
      4     print(n, result)
      5     nq_complexity.append(result[1])

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
      7     safe_calls += 1
      8     if queen_safe(row, qsofar):
----> 9         result, ncalls = nqueens(n, qsofar + [row])
     10         safe_calls += ncalls
     11         if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
      7     safe_calls += 1
      8     if queen_safe(row, qsofar):
----> 9         result, ncalls = nqueens(n, qsofar + [row])

```

```

10         safe_calls += ncalls
11         if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
7         safe_calls += 1
8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
10             safe_calls += ncalls
11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
7         safe_calls += 1
8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
10             safe_calls += ncalls
11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
7         safe_calls += 1
8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
10             safe_calls += ncalls
11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
7         safe_calls += 1
8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
10             safe_calls += ncalls
11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
7         safe_calls += 1
8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
10             safe_calls += ncalls
11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
7         safe_calls += 1
8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
10             safe_calls += ncalls
11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
7         safe_calls += 1
8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
10             safe_calls += ncalls
11             if result:

```

```
11         if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
    7         safe_calls += 1
    8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
    10             safe_calls += ncalls
    11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
    7         safe_calls += 1
    8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
    10             safe_calls += ncalls
    11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
    7         safe_calls += 1
    8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
    10             safe_calls += ncalls
    11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
    7         safe_calls += 1
    8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
    10             safe_calls += ncalls
    11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
    7         safe_calls += 1
    8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
    10             safe_calls += ncalls
    11             if result:

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
    7         safe_calls += 1
    8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
    10             safe_calls += ncalls
    11             if result:
```

```

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
      7         safe_calls += 1
      8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
      10             safe_calls += ncalls
      11             if result:

```

```

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
      7         safe_calls += 1
      8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
      10             safe_calls += ncalls
      11             if result:

```

```

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
      7         safe_calls += 1
      8         if queen_safe(row, qsofar):
----> 9             result, ncalls = nqueens(n, qsofar + [row])
      10             safe_calls += ncalls
      11             if result:

```

```

<ipython-input-11-0b6e55dc5c78> in nqueens(n, qsofar)
      6         for row in range(n):
      7             safe_calls += 1
----> 8             if queen_safe(row, qsofar):
      9                 result, ncalls = nqueens(n, qsofar + [row])
      10                 safe_calls += ncalls

```

```

<ipython-input-7-85d5bce565ef> in queen_safe(row, qsofar)
      10             return False
      11             # diagonal attack
----> 12             if abs(prow-row) == col-pcol:
      13                 return False
      14             # no problems with any existing queens

```

KeyboardInterrupt:

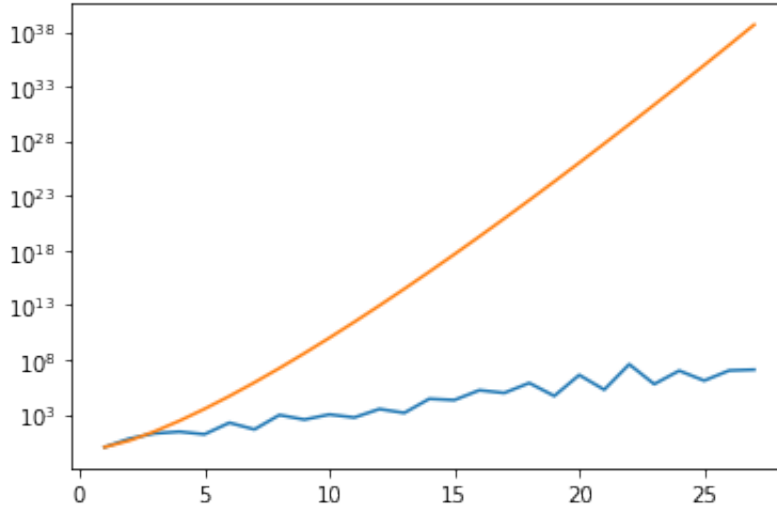
```

In [18]: %matplotlib inline
import matplotlib.pyplot as plt

```

```
In [26]: xaxis = list(range(1, len(nq_complexity)+1))
plt.yscale('log')
plt.plot(xaxis, nq_complexity)
plt.plot(xaxis, [n**n for n in xaxis])
```

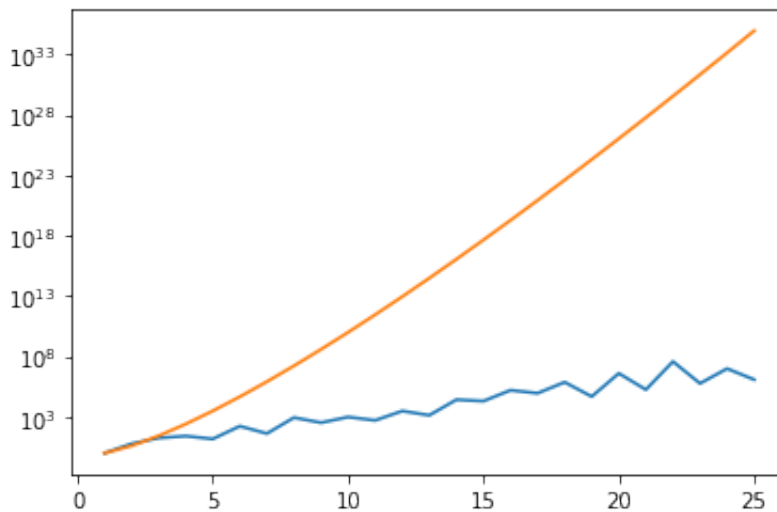
```
Out[26]: [<matplotlib.lines.Line2D at 0x121499a90>]
```



```
In [20]: xaxis = list(range(1, len(nq_complexity)+1))
```

```
In [22]: plt.yscale('log')
plt.plot(xaxis, nq_complexity)
plt.plot(xaxis, [n**n for n in xaxis])
```

```
Out[22]: [<matplotlib.lines.Line2D at 0x11c3abd90>]
```



```
In [53]: words = {"this", "is", "a", "hard", "course", "aha", "i", "a", "ah", "ha",
"his", "sis", "our", "ours", "har"}
```

```
In [54]: def segment(s, n=0):
          print(f"segment {s[n:]}")
          if n == len(s):
              return True
          for i in range(1, len(s)-n+1):
              if s[n:n+i] in words:
                  if segment(s,n+i):
                      return True
          return False
```

```
In [57]: segment("thisisahardcourse")
```

```
segment thisisahardcourse
segment isahardcourse
segment sahardcourse
segment ahardcourse
segment hardcourse
segment rdcourse
segment dcourse
segment course
segment
```

```
Out[57]: True
```

```
In [58]: segment("thisisahardcourseq")
```

```
segment thisisahardcourseq
segment isahardcourseq
segment sahardcourseq
segment ahardcourseq
segment hardcourseq
segment rdcourseq
segment dcourseq
segment courseq
segment q
segment ardcourseq
segment rdcourseq
segment rdcourseq
```

```
Out[58]: False
```